

# High-throughput computational exploration of ternary $M_3A_2X$ phases: Stability, properties, and exfoliation potential

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$M_3A_2X$  phase is a type of ternary layered MAX-phase-like materials. To date, only four stable  $M_3A_2X$  phases have been discovered. In this research, high-throughput density functional theory calculations were employed to systematically identify stable  $M_3A_2X$  phases and then predict their properties. Starting from 240 possible compositions and 51 structural models for each composition, 12  $M_3A_2X$  phases successfully passed three rounds of stability assessment (thermodynamic, dynamic, and mechanical stabilities) and thus are stable. Crystal structures of stable  $\text{Sc}_3\text{S}_2\text{C}$ ,  $\text{Y}_3\text{S}_2\text{C}$  and  $\text{Y}_3\text{Se}_2\text{C}$  are novel and different from those of synthesized  $M_3A_2X$  phases. The electrical conductivities of the 12  $M_3A_2X$  phases are generally superior to those of corresponding classic  $M_2AX$  phases, while their mechanical properties are slightly inferior. Through the comparison of bond strengths using the crystal orbital Hamilton population analysis, it has been discovered that  $M_3A_2X$  phases have a greater tendency to exfoliate into 2D MXenes than  $M_2AX$  phases. Among them, the  $\text{Zr}_3\text{Se}_2\text{C}$ ,  $\text{Zr}_3\text{S}_2\text{C}$ , and  $\text{Sc}_3\text{S}_2\text{C}$  phases exhibit the highest exfoliation potential. This study provides a comprehensive understanding of  $M_3A_2X$  phases, laying a solid foundation for future experimental synthesis and technological applications.

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## I. INTRODUCTION

MAX phases are a large family of ternary layered compounds with a general chemical formula  $M_{n+1}AX_n$  ( $n = 1, 2, 3$ ), where  $M$  represents an early transition metal,  $A$  denotes an A-group element (primarily groups 13–16 in the periodic table), and  $X$  indicates C or N [1]. These compounds exhibit a nanolaminated architecture (see Fig. 1), characterized by  $M_{n+1}X_n$  layers interspersed with  $A$ -atom layers. The robust covalent  $M$ - $X$  bonds are responsible for ceramic-like properties such as high stiffness, excellent chemical resistance, and low thermal expansion coefficients [1–4]. In contrast, the relatively weaker  $M$ - $A$  bonds endow the material with superior thermal and electrical conductivity, enhanced damage tolerance, thermal shock resistance, and good machinability [1–4].

Two MAX phases ( $\text{Ti}_2\text{SC}$  and  $\text{Zr}_2\text{SC}$ ) were first synthesized in 1960 [5]. Subsequently, Nowotny and co-workers reported more than 30 MAX phases including  $\text{Ti}_2\text{AlN}$ ,  $\text{V}_2\text{AlC}$ ,  $\text{Zr}_2\text{InN}$ , and  $\text{Nb}_2\text{InC}$  [1]. Since Barsoum synthesized the dense  $\text{Ti}_3\text{SiC}_2$  phase in 1996 and highlighted its outstanding properties, MAX phases have gradually attracted increasing research interest [6,7]. Especially since 2011, when two-dimensional (2D) MXene was first produced by etching MAX phases [8], the synthesis of new MAX phases has gained greater practical significance. Since 2019, more than 170 new

MAX phases (including solid solutions) have been discovered [4]. Notably, in 2023 alone, 69 new MAX phases were identified [4]. Currently, at least 342 MAX phases (including 124 ternary stoichiometric ones) have been successfully synthesized [4].

One important direction for developing new MAX phases is to expand the range of  $M$ ,  $A$ , and  $X$  elements. A so-called top-down approach (including molten salt method and elemental exchange reaction) through substitution of the  $A$  layers is employed to synthesize new MAX phases. Using the molten salt substitution method, Huang's group identified new MAX phases with  $A = \text{Fe}, \text{Co}, \text{Ni}, \text{Cu}$ , and  $\text{Zn}$  elements [9–13]. Thin films of MAX phases containing noble metals have been achieved through thermally induced exchange reactions by replacement of Al, Si, and Ga with Au or Ir [14–17]. Furthermore, MAX phases with  $A = \text{Se}$  and  $\text{Te}$  have been reported [18–21]. In the past two years, spark plasma sintering has been used to successfully obtain a series of new MAX phases with Ga, Pb, In, Sb, and Cd as the  $A$  element [22–26]. Recently, MAX phases with boron as the  $X$  element have also been discovered experimentally [18,21,27–30].

Expanding the structural diversity of MAX phases is also a crucial approach to developing novel phases. Crystal structures of the classic  $M_{n+1}AX_n$  phases with  $n = 1, 2, 3$  exhibit a hexagonal crystal system with a  $P6_3/mmc$  space group, which are presented in Fig. 1. The crystal structures in these classic MAX phases consist of only one  $A$  layer inserted between adjacent  $M_{n+1}X_n$  blocks. In 2015 the successful synthesis of  $\text{Mo}_2\text{Ga}_2\text{C}$  marked the beginning of MAX phases with double  $A$  layers, in which two Ga layers

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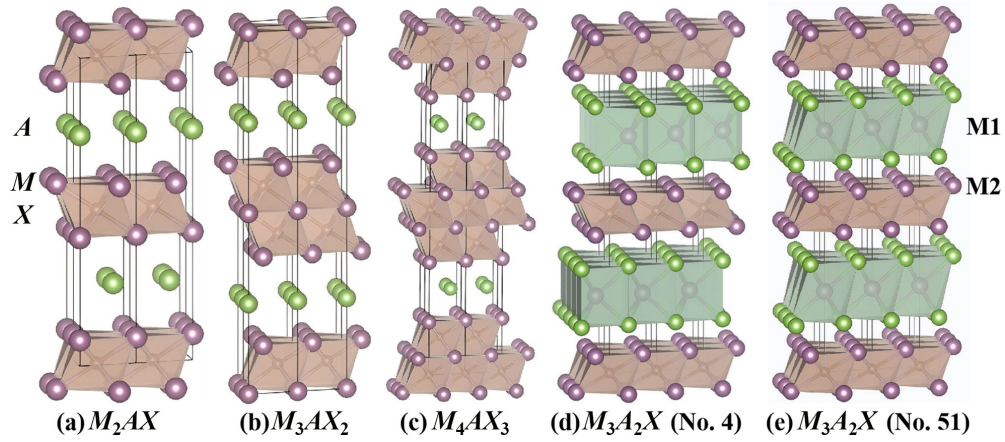


FIG. 1. Crystal structures of (a)  $M_2AX$ , (b)  $M_3AX_2$ , (c)  $M_4AX_3$ , (d), and (e)  $M_3A_2X$  phases.

exist between the neighboring  $Mo_2C$  blocks. To date, four  $MAX$  phases of  $Ti_3Cd_2C_2$  [13],  $Ti_3Au_2C_2$  [14,15],  $Ti_2Au_2C$  [15], and  $Nb_2Bi_2C$  [13] with double A layers have also been synthesized. Recently, Chen *et al.* synthesized a new series of  $Nb_3As_2C$ ,  $V_3As_2C$ ,  $Nb_3P_2C$ , and  $Ta_3P_2C$   $MAX$  phases using molten-salt sintering and solid-state synthesis methods [31,32]. These phases have the chemical formula of  $M_3A_2X$ , which is different from traditional  $M_{n+1}AX_n$ . Figure 1(d) shows the crystal structure of the synthesized  $M_3A_2X$  phase. The distinguishing feature in  $M_3A_2X$  crystal structure is the insertion of an  $A$ - $M$ - $A$  block, rather than a single or double  $A$ -layer, between neighboring  $M$ - $X$ - $M$  blocks. The novel structure has brought about changes in performance. The average linear thermal expansion coefficients of  $M_3A_2X$  phases are measured as the lowest among the reported values of  $MAX$  phases [33]. The experimental bulk modulus of  $Nb_3As_2C$  reaches up to 225 GPa [31], close to the highest values observed in  $MAX$  phases [34]. Elastic, thermal, and lattice dynamic properties of these four  $M_3A_2X$  phases were also investigated through first-principles calculations [35].

To date, 67, 15, and 7 stoichiometric members have been synthesized for the classic  $M_2AX$ ,  $M_3AX_2$ , and  $M_4AX_3$  phases, respectively [4]. For the  $M_3A_2X$  phases, only the four phases mentioned above have been synthesized. It is anticipated that more stable  $M_3A_2X$  phases can be discovered through expanding the range and/or considering more combinations of the  $M$ ,  $A$ , and  $X$  elements. The combination of numerous  $M$ ,  $A$  and  $X$  elements will result in a large number of  $M_3A_2X$  candidates. It is impractical to evaluate the potential of large  $M_3A_2X$  candidates through experimental methods. High-throughput calculations [36] are a powerful tool for screening and identifying stable phases from a vast number of hypothetical candidates with similar crystal structures. This approach has proven successful in predicting new stable  $M_2AX$ ,  $M_3AX_2$ , and  $M_4AX_3$  phases [4,37–44]. For example, Ashton *et al.* screened a total of 3140 pure  $M_2AX$  phases and their solid solutions that can be easily synthesized in experiments from 10 530 candidates [39]. Similar work has also been done by Ohmer and colleagues, who identified 82 stable  $M_2AX$  phases from 1080 possible compositions [44]. Except for identifying stable  $M_2AX$  phases, high-throughput searches based on first-principles calculations were also

conducted on  $M_3AX_2$  and  $M_4AX_3$  phases [4,40], as well as the solid solution  $MAX$  phases [43].

Given that only 4  $M_3A_2X$  phases have been synthesized so far, there is a demand for more stable  $M_3A_2X$  compositions. In this study, we employed a high-throughput computational method to systematically predict and identify stable phases in  $M_3A_2X$ . The electrical and mechanical properties of the predicted stable  $M_3A_2X$  phases were determined and compared with those of traditional  $M_2AX$  phases. Finally, the possibility of exfoliating the  $M_3A_2X$  phases into 2D MXenes was evaluated, which could guide the  $M_3A_2X$  materials for specific applications.

## II. COMPUTATIONAL DETAILS

First-principles calculations based on density functional theory (DFT) [45,46] were employed, as implemented within the Vienna Ab-initio Simulation Package (VASP) [47]. In structure relaxation, full optimization was adopted, meaning that both the atomic positions and lattice constants were relaxed simultaneously. The generalized gradient approximation (GGA), parameterized by Perdew-Burke-Ernzerhof (PBE), was taken to calculate the exchange and correlation energy of electrons. The electron-ion interaction was processed by the projector augmented wave (PAW) method [48,49] with an energy cutoff of 520 eV. The first Brillouin zone integration used the special K-point method in the form of Monkhorst-Pack (MP) [50] with a K-point accuracy of  $2\pi \times 0.03 \text{ \AA}^{-1}$ . The convergence accuracy of the iteration in the self-consistent field (SCF) of the electronic step was  $1.0 \times 10^{-5}$  eV/atom, and the conjugate gradient algorithm (CG) was employed for ion optimization with an energy convergence criterion of  $1.0 \times 10^{-4}$  eV/atom. The phonon spectrum was calculated using the finite displacement method, which was a joint calculation performed by VASP and PHONOPY software [51,52]. The Gibbs free energies at finite temperature was obtained by the quasi-harmonic approximation (QHA) method through VASP-PHONOPY. The elastic constants were calculated using the stress-strain method [53]. The crystal orbital Hamilton population (COHP) analysis was carried out using the LOBSTER code [54]. The competing phases considered herein are sourced from the

| I A |      |       |          |     |      |       |          |    |          |     |       |    |      | VIII A |     |       |    |   |   |   |   |   |    |
|-----|------|-------|----------|-----|------|-------|----------|----|----------|-----|-------|----|------|--------|-----|-------|----|---|---|---|---|---|----|
| H   | II A |       | <i>M</i> |     |      |       | <i>A</i> |    | <i>X</i> |     | III A |    | IV A | V A    | VIA | VII A | He |   |   |   |   |   |    |
| Li  | Be   |       |          |     |      |       |          |    |          |     |       |    |      |        |     |       |    | B | C | N | O | F | Ne |
| Na  | Mg   | III B | IV B     | V B | VI B | VII B | VIII     |    |          | I B | II B  | Al | Si   | P      | S   | Cl    | Ar |   |   |   |   |   |    |
| K   | Ca   | Sc    | Ti       | V   | Cr   | Mn    | Fe       | Co | Ni       | Cu  | Zn    | Ga | Ge   | As     | Se  | Br    | Kr |   |   |   |   |   |    |
| Rb  | Sr   | Y     | Zr       | Nb  | Mo   | Tc    | Ru       | Rh | Pd       | Ag  | Cd    | In | Sn   | Sb     | Te  | I     | Xe |   |   |   |   |   |    |
| Cs  | Ba   | La-Lu | Hf       | Ta  | W    | Re    | Os       | Ir | Pt       | Au  | Hg    | Tl | Pb   | Bi     | Po  | At    | Rn |   |   |   |   |   |    |
| Fr  | Ra   | Ac-Lr | Rf       | Db  | Sg   | Bh    | Hs       | Mt | Ds       | Rg  | Cn    | Nh | Fl   | Mc     | Lv  | Ts    | Og |   |   |   |   |   |    |

FIG. 2. Elements considered for  $M$ ,  $A$ , and  $X$  atoms in the  $M_3A_2X$  phases.

Materials Project [55] and the Open Quantum Materials Database (OQMD) [56,57], which were reoptimized in this paper to get accurate energies.

### III. RESULTS AND DISCUSSION

#### A. Elemental selection and structural model

Both the common elements present in classic  $MAX$  phases and the new elements found in the  $MAX$  phases reported recently [10,14–17,58] were considered. The element search space with 12  $M$  elements (Sc, Ti, V, Cr, Mn, Y, Zr, Nb, Mo, Hf, Ta, W) and 20  $A$  elements (Al, Si, P, S, Cu, Zn, Ga, Ge, As, Se, Ag, Cd, In, Sn, Sb, Te, Au, Tl, Pb, Bi) is depicted in Fig. 2. Since binary metal nitrides act as robust and stable competing phases [38], the number of stable  $MAX$  phases with  $X = N$  is significantly smaller compared to those with  $X = C$  [4]. In this work, we restrict the  $X$  element to carbon only. With this combination of elemental components, there are  $12 \times 20 \times 1 = 240$  possible  $M_3A_2X$  compositions.

Although the four synthesized  $M_3A_2X$  phases share the same structure [Fig. 1(d)], it remains questionable whether the 240  $M_3A_2X$  compositions would exhibit the same structure. Actually polymorphism phenomenon has been observed in some  $MAX$  phases, such as  $Ti_4GaC_3$  [59],  $Ta_4AlC_3$  [60], and  $Mo_2Ga_2C$  [61–63]. Thus in this paper, we investigated various crystal structures for each  $M_3A_2X$  composition. First, a 12-atom unit cell containing two  $M_3A_2X$  chemical formulas was adopted, which is commonly seen in classic  $MAX$  phases. Second, three stacking models along the  $c$  direction of adjacent  $M-X-M$  blocks, namely, I, II, and III [depicted in Fig. 3(a)], were taken into account. Third, considering different positions of  $A$  and  $M$  atoms of  $A-M-A$  block in the  $a-b$  plane, four models [shown in Fig. 3(b)] of a  $A-M-A$  block can be constructed: (1) The  $A$ ,  $M$ , and  $A$  atoms occupy the same position, forming a straight chainlike structure. (2) One  $A$  atom and the  $M$  atom share the same position, while the other  $A$  atom occupies a different position, resulting in the  $A$  atoms forming a tetrahedral structure, with the  $M$  atom locating at the center, (3) When the  $A$  atoms in the upper and lower layers occupy the same position, they form a trigonal

prism, with the  $M$  atom locating at the center, (4) In the case where the  $A$ ,  $M$ , and  $A$  atoms occupy different positions, the  $A$  atoms form an octahedral structure, with the  $M$  atom at the center. Last, we positioned each of the four  $A-M-A$  models at different locations between adjacent  $M-X-M$  blocks of the three stacking models in Fig. 3(a). This process yielded a total of 81  $M_3A_2X$  configurations. After carefully examining the 81 configurations, 30 of them had atomic arrangements identical to those of others. Therefore, there are actually only 51 distinct configurations, which were presented in Fig. S.1 (see the Supplemental Material [64]). The quantities of each type of  $M_3A_2X$  configurations, which were formed by combining the four  $A-M-A$  models with the three  $M-X-M$  stacking models, are presented in Fig. 3(c).

#### B. Lowest-energy configuration

All 51 crystal structures for each of the 240 possible  $M_3A_2X$  compositions were fully relaxed. A total of  $240 \times 51 = 12\,240$  structural optimization calculations were thus carried out. Because atoms were positioned at highly symmetric sites in each of the 51 constructed structures, all initial structures maintained their original configurations after optimization and only minor adjustments were made to atomic positions to optimize interatomic distances.

The lowest-energy configuration of each  $M_3A_2X$  composition is the most stable thermodynamically, which is summarized in Fig. 4, and the detailed information about structure and energy is presented in Table S.1 [64]. It can be found that the model-II stacking of  $M-X-M$  block, as well as the chainlike and tetrahedral structures of  $A-M-A$  block, are unfavorable for all  $M_3A_2X$  compositions (except for  $Sc_3Cu_2C$ ). Nearly half (118 out of 240) of the  $M_3A_2X$  phases have their lowest-energy structure in the form of the No. 4 configuration in Fig. S.1 [64]. The  $A$  element in these 118  $M_3A_2X$  phases is mainly found in the main groups. The lowest-energy structure of all four synthesized  $M_3A_2X$  phases ( $Nb_3As_2C$ ,  $V_3As_2C$ ,  $Nb_3P_2C$ , and  $Ta_3P_2C$ ) falls into this configuration, which is in accordance with previous experimental results [31]. The second most lowest-energy structure is the

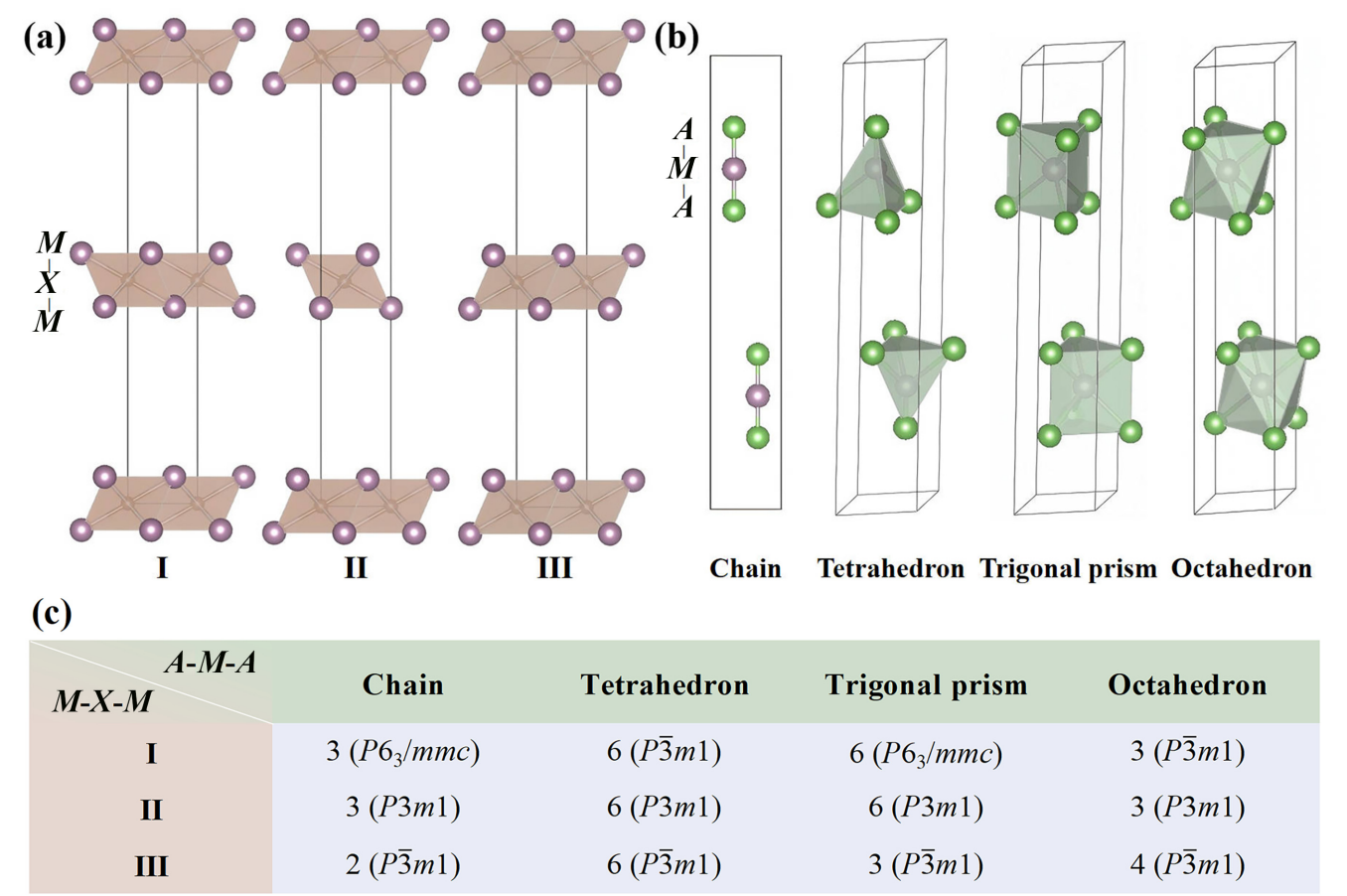


FIG. 3. (a) Three stacking models of the  $M-X-M$  block. (b) Four models of the  $A-M-A$  block. (c) Quantities of each type of  $M_3A_2X$  configurations. The corresponding space group is shown in the parentheses.

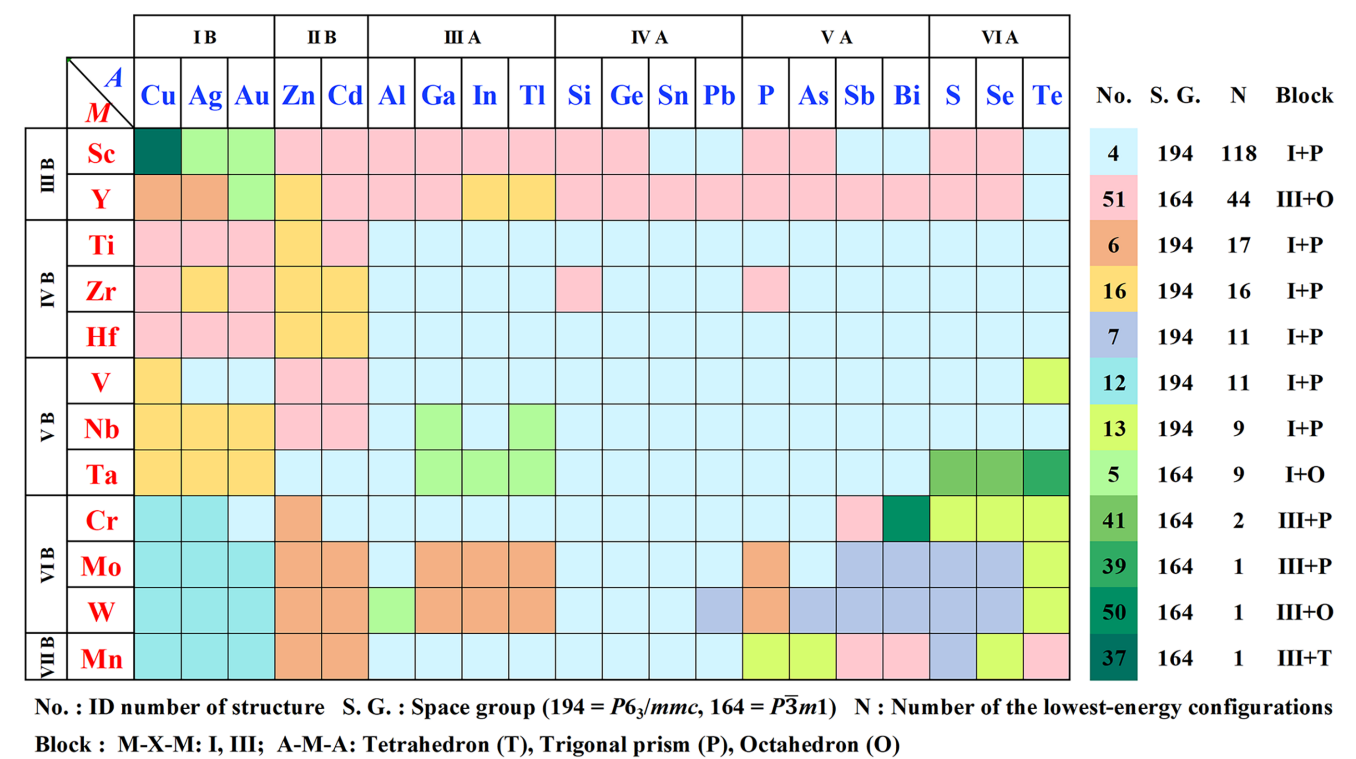


FIG. 4. Distribution and statistics of the lowest-energy configuration of each  $M_3A_2X$  composition.

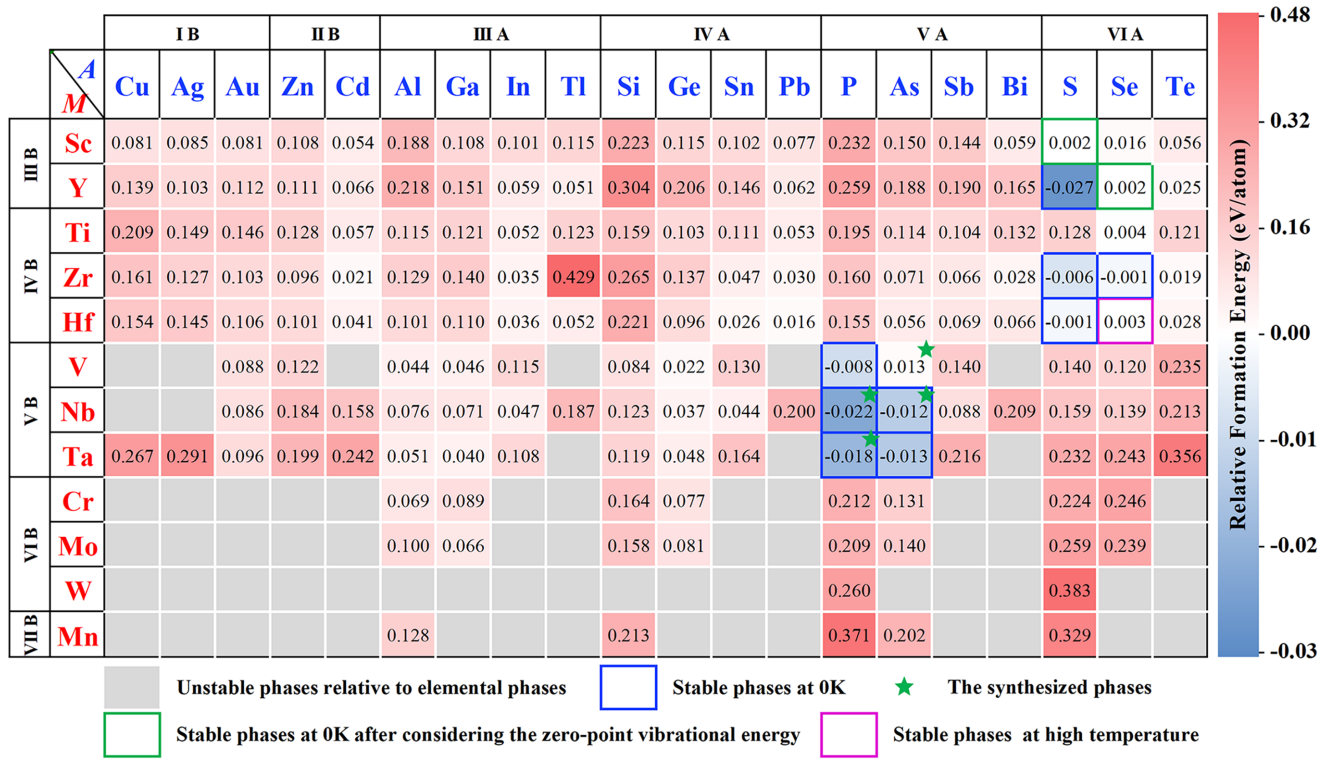


FIG. 5. Heatmaps of the formation energies  $E_{\text{comp}}$  of  $M_3A_2X$  phases relative to all competing phases. The gray boxes represent unstable phases relative to elemental phases. Thermodynamic stability of  $M_3A_2X$  phases is marked with different colors and symbols.

No. 51 configuration in Fig. S.1 [64], which is primarily found where the  $M$  element is from Group IIIB and the  $A$  element is from a transition metal group. Over half of the  $M_3A_2X$  phases do not have the experimentally synthesized No. 4 configuration as their lowest-energy structure. This validates the necessity of the methodology which involves taking various structures into account during identifying the lowest-energy structure.

The No. 4 and 51 configurations account for more than two-thirds of the lowest-energy structures. These two crystal structures are given in Figs. 1(d) and 1(e). Other configurations with smaller proportions are not described in detail here. The No. 4 configuration belongs to the  $P6_3/mmc$  space group, which is formed by placing the  $A$ - $M$ - $A$  edge-sharing trigonal prism into the  $M$ - $X$ - $M$  stacking model-I. The No. 51 configuration possesses the  $P\bar{3}m1$  space group and is formed through the combination of the  $M$ - $X$ - $M$  stacking model-III and the  $A$ - $M$ - $A$  edge-sharing octahedron.

### C. Phase stability

The stability of the lowest-energy configurations for the 240  $M_3A_2X$  compositions was assessed through the next three rounds: thermodynamic stability, dynamic stability, and mechanical stability.

#### 1. Thermodynamic stability

The calculation of thermodynamic stability is crucial for discovering novel phases. Thermodynamic stability evaluates a compound's resistance to decomposition into any combination of elemental, binary, or other ternary phases, thus the

candidate compound should possess a lower energy than any combination of all potential competing phases. For ternary compounds like  $M_3A_2X$ , there can be numerous combinations of competing phases. Especially for 240  $M_3A_2X$  compositions in this work, it should take considerable time and effort to investigate the thermodynamic stability against all competing phases. Thus as an initial screening, we first investigated the thermodynamic stability of these 240  $M_3A_2X$  compositions against their constituent elemental phases.

The formation energy of a  $M_3A_2X$  phase against its constituent elemental phases is calculated by the equation  $E_f = 6E(M_3A_2X) - 3E(M) - 2E(A) - E(X)$ , where  $E(M_3A_2X)$  is the total energy (in eV/atom) of the  $M_3A_2X$  phase, and  $E(M)$ ,  $E(A)$ , and  $E(X)$  are the total energy (in eV/atom) of the  $M$ ,  $A$ , and  $X$  elemental phases in their ground-state bulk structures. A negative  $E_f$  value indicates the  $M_3A_2X$  phase is thermodynamically stable against decomposition into the  $M$ ,  $A$ , and  $X$  elemental phases. The calculated  $E_f$  values of the 240  $M_3A_2X$  compositions are summarized in Table S.2 [64]. We predict 68  $M_3A_2X$  compositions with positive  $E_f$  values to be thermodynamically unstable. These unstable  $M_3A_2X$  phases (illustrated in Fig. 5) are primarily observed for the  $M$  atom in the VIIIB and VIB groups (especially when the  $A$  atom in the 6<sup>th</sup> period). The reason behind the instability will be discussed later in this paper.

Subsequently, thermodynamic stability of the remaining 172  $M_3A_2X$  compositions was assessed by calculating their formation energies  $E_{\text{comp}}$  relative to all competing phases using the equation  $E_{\text{comp}} = E(M_3A_2X) - E(\text{set of the most competing phases})$ , where  $E(M_3A_2X)$  is the total energy of  $M_3A_2X$  phase and  $E(\text{set of the most competing phases})$  is

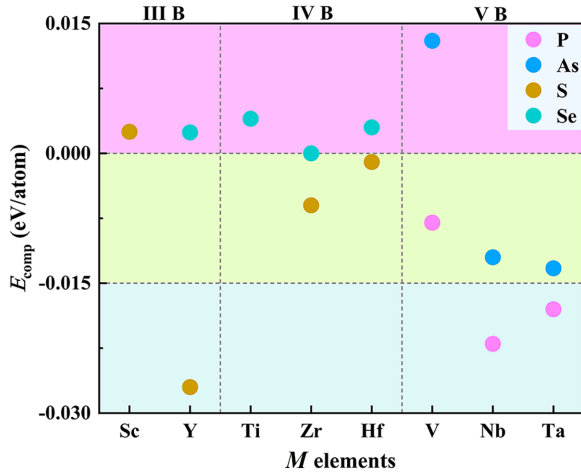


FIG. 6.  $E_{\text{comp}}$  values of nine stable and five metastable  $M_3A_2X$  phases.

the total energy of the set of the most competing phases with the same stoichiometry as the  $M_3A_2X$  phase. Identifying the set of the most competing phases out of all competing phases is the crucial step. In this paper, the set of the most competing phases, referred to as equilibrium simplex, is determined through a linear optimization procedure [38,65]. This approach has been demonstrated to be effective in both validating experimentally known MAX phases and predicting the existence of new ones [38–41,43,65–68].

The calculated  $E_{\text{comp}}$  values and the set of the most competing phases of the 172  $M_3A_2X$  phases are listed in Table S.3 [64]. A heatmap (Fig. 5) of the calculated  $E_{\text{comp}}$  can visually display the stability distribution of  $M_3A_2X$  phases. Only nine  $M_3A_2X$  phases ( $V_3P_2C$ ,  $Nb_3P_2C$ ,  $Nb_3As_2C$ ,  $Ta_3P_2C$ ,  $Ta_3As_2C$ ,  $Y_3S_2C$ ,  $Zr_3S_2C$ ,  $Zr_3Se_2C$ , and  $Hf_3S_2C$ ) have negative  $E_{\text{comp}}$  and are therefore thermodynamically stable. From the values of the  $E_{\text{comp}}$  and the distribution of the stable phases, it can be seen that the stability of the  $M_3A_2X$  phases has a local characteristic and is related to the positions of the  $M$  and  $A$  atoms. The nine  $M_3A_2X$  phases are mainly distributed in two regions. One is formed when the  $M$  atom is a group-VB element (V, Nb, Ta) and the  $A$  atom is a P or As element in the VA group. Another region of stable  $M_3A_2X$  phases located near the upper right corner is formed by  $M = Y, Zr$ , and  $Hf$  and  $A = S$  and  $Se$ . According to radius ratio rule in chemistry, the radius ratio of  $M$  to  $A$  atoms plays a significant role in the stability of the  $A$ - $M$ - $A$  octahedron and prism in Figs. 1(d) and 1(e). Some papers also report that the valence electron and atomic size of the elements are major factors for the stability of MAX phases [39,40,44,69]. Thus, only the  $M_3A_2X$  phases with appropriate  $M$  and  $A$  atoms are stable.

The  $E_{\text{comp}}$  value (i.e. the distance to convex hull) of a compound can be thought as the thermodynamic driving force for the most stable competing phase to synthesize this compound. More negative  $E_{\text{comp}}$  means an easier tendency for synthesis. The  $E_{\text{comp}}$  values of nine stable and five metastable ( $0 < E_{\text{comp}} < 0.015$  eV/atom)  $M_3A_2X$  phases are illustrated in Fig. 6. The synthesized  $Nb_3As_2C$ ,  $Nb_3P_2C$ , and  $Ta_3P_2C$  indeed possess relatively lower  $E_{\text{comp}}$ . In addition, the  $E_{\text{comp}}$

TABLE I. Statistics about the most competing phases for the 172  $M_3A_2X$  phases.

| Competing phases | Types      | Numbers | Total |
|------------------|------------|---------|-------|
| Elementary phase | $M$        | 10      | 52    |
|                  | $A$        | 24      |       |
|                  | $X$        | 18      |       |
| Binary phase     | $M$ - $X$  | 110     | 310   |
|                  | $M$ - $A$  | 199     |       |
|                  | $A$ - $X$  | 1       |       |
| Ternary phase    | MAX phases | 61      | 92    |
|                  | Others     | 31      |       |
| Total            |            |         | 454   |

values of predicted  $Y_3S_2C$  and  $Ta_3As_2C$  are also relatively low and should be more readily synthesizable. In particular,  $Y_3S_2C$  has the most negative  $E_{\text{comp}}$ . Therefore, experimenters can focus on these two phases as the targets in the future.

Although our calculations reflect the thermodynamic stability of  $M_3A_2X$  phases at 0 K, the results still match the experimental findings quite well. Three ( $Nb_3As_2C$ ,  $Nb_3P_2C$ , and  $Ta_3P_2C$ ) out of four phases synthesized experimentally [31] were calculated to be thermodynamically stable, which demonstrates the reliability of our calculations. The only discrepancy is  $V_3As_2C$ . The raw materials used for the synthesis of  $V_3As_2C$  are VAs, V, and graphite powders [31]. We calculated the formation energy for the reaction  $2VAs + V + C = V_3As_2C$  to be  $-0.172$  eV/atom, indicating that this reaction path is possible. However,  $V_3As_2C$  is unstable compared to the most stable competing phase ( $VAs_2 + V_2AsC + V_5As_4$ ,  $E_{\text{comp}} = 0.013$  eV/atom). Therefore, the synthesized  $V_3As_2C$  has a tendency to decompose in thermodynamics. In fact, some unknown phases were observed in the synthesized  $V_3As_2C$  samples [31], confirming the instability of  $V_3As_2C$ .

Next, we will analyze the set of the most competing phases listed in Table S.3 [64]. For the 172  $M_3A_2X$  phases, none of the set of the most competing phases consists solely of three elemental materials, which indicates that it is inaccurate to judge the thermodynamic stability merely using the formation energy relative to elemental materials, as reported in [4,40,70,71]. We conducted a statistical analysis (as shown in Table I) of the most competing phases for the 172  $M_3A_2X$  phases. Among the 454 occurrences of competing phases, elemental materials appear only 52 times. In ternary competing phases, MAX phases occurred 61 times, and other ternary phases occurred 31 times. Binary compounds are the most frequently occurring and account for about two-thirds. Among the binary competing phases, roughly two-thirds are  $M$ - $A$  compounds, approximately one-third are  $M$ - $X$  compounds, and  $A$ - $X$  compounds occur only once. Thus, binary  $M$ - $A$  and  $M$ - $X$  phases emerge as the main rivals competing for stability with the  $M_3A_2X$  phase.

In previous studies on predicting MAX phases, a common mistake was to ignore other series of MAX phases as competing phases. In recent years, newly synthesized or predicted MAX phases have been emerging continuously, and they are not promptly included in the Materials Project and OQMD databases. Therefore, in addition to the MAX phases in these

two databases, stable  $M_3A_2X$  phases reported recently [4,40,44] were manually considered as competing phases. This operation has indeed changed the stability of some  $M_3A_2X$  phases. We take the  $Nb_3In_2C$  as an example. If we consider only the phases in Materials Project and OQMD databases,  $Nb_3In_2C$  with  $E_{comp} = -0.001$  eV/atom is predicted to be stable with Nb, In, and  $Nb_2C$  as the most competing phases. However, if the stable  $Nb_2InC$  phase [4] is included in the assessment of stability,  $Nb_3In_2C$  with  $E_{comp} = 0.047$  eV/atom becomes unstable with Nb,  $Nb_2In_5$  and  $Nb_2InC$  as the most competing phases. This indicates that the stability of  $M_3A_2X$  phases could be overestimated if other series of  $M_3A_2X$  phases are neglected as competing phases.

Given that typical synthesis of bulk  $M_3A_2X$  phases is conducted at around 1500 °C, the lattice vibrational effect at high temperatures is not negligible and ought to be taken into account for precise stability prediction. Thermodynamic stability at a given temperature can be determined by calculating formation energy relative to the set of the most competing phases at the same temperature. However, in most cases the set of the most competing phases at high temperatures is the same as that at 0 K [42]. Therefore, thermodynamic stability of the  $M_3A_2X$  phase at a given temperature ( $T$ ) is assessed using the equation  $E_{comp}(T) = E(M_3A_2X, T) - E(\text{set of the most competing phases}, T)$ , where  $E(M_3A_2X, T)$  is the total energy of  $M_3A_2X$  phase and  $E(\text{set of the most competing phases}, T)$  is the total energy of the set of the most competing phases (the same as that at 0 K) at this temperature of  $T$  K.

The impact of temperature on stability can be twofold. Phases that were formerly stable may become unstable, while phases that were initially unstable could turn stable. When the absolute value of the formation energy ( $|E_{comp}|$ ) of a phase gets closer to 0, there is a high probability that the stability of this phase will be altered at elevated temperatures. Vibrational and heat capacity effects at 298 K alter  $E_{comp}$  by about 0.007 eV/atom, with entropy's influence growing at higher temperatures [72]. However, these thermal impacts vary significantly between materials, and some show minimal changes [73]. We first took the eight  $M_3A_2X$  phases within the range of  $|E_{comp}| < 0.010$  eV/atom as examples to investigate the influence of temperature. From the curves of calculated  $E_{comp}$  versus temperature plotted in Fig. 7, it can be observed that when the temperature increases from 0 K to 1800 K, the  $E_{comp}$  values of 7  $M_3A_2X$  phases except  $Y_3Se_2C$  change by less than 0.010 eV/atom. This indicates that using an  $E_{comp}$  threshold of 0.010 eV/atom is sufficient for studying the effect of temperature on the stability of  $M_3A_2X$  phases. To ensure scientific rigor, we increased the tolerance of  $E_{comp}$  and ultimately set the  $E_{comp}$  threshold at 0.015 eV/atom. Seen from Fig. 6, there are six stable and five metastable  $M_3A_2X$  phases at 0 K that meet the condition of  $|E_{comp}| < 0.015$  eV/atom. The curves of calculated  $E_{comp}$  versus temperature for these 11  $M_3A_2X$  phases are plotted in Fig. 7. We noticed that all six stable phases keep steady within the entire temperature range. The  $Hf_3Se_2C$  becomes stable when the temperature is higher than around 1000 K.  $V_3As_2C$  and  $Ti_3Se_2C$  remain unstable during the whole temperature range. After considering only the zero-point vibrational energy, the formation energies of  $Sc_3S_2C$  and  $Y_3Se_2C$  shift from positive to negative, making them the ground-state stable phases at 0 K. However, the

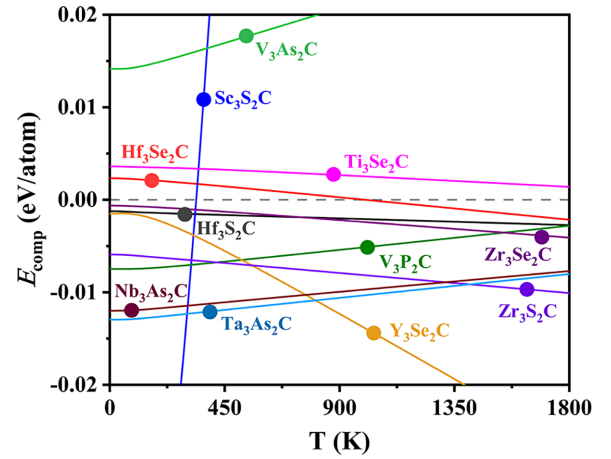


FIG. 7.  $E_{comp}$  values of  $M_3A_2X$  phases as a function of temperature.

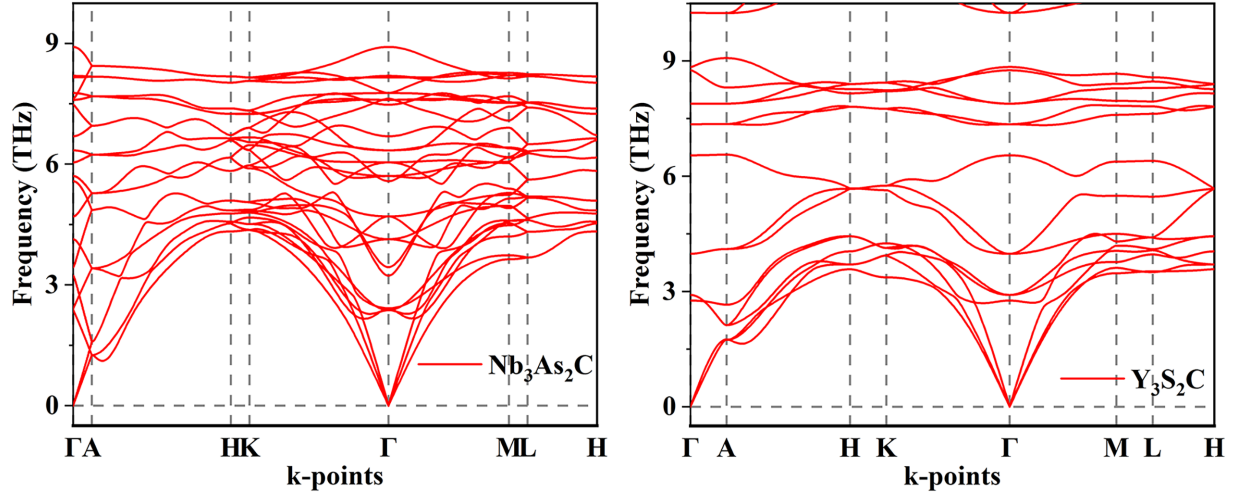
formation energy of  $Sc_3S_2C$  rises rapidly with the increase of temperature and turns from negative to positive at approximately 340 K, meaning that the phase becomes unstable. The variation trend of the  $E_{comp}$  of  $Sc_3S_2C$  is strange and different with other  $M_3A_2X$  phases. To identify the reason, we have plotted the curves of free energy versus temperature for all four stable  $M_3A_2X$  phases with  $A = S$  and their corresponding competing phases (see Fig. S.2 [64]). It can be found that the free energy trends of all compounds are quite similar, and only the free energy of  $Sc_5S_4C$  decreases rapidly with the increase of temperature. Therefore, it can be concluded that the rapid increase in  $E_{comp}$  for  $Sc_3S_2C$  is caused by the rapid decrease in the free energy of the competing phase  $Sc_5S_4C$ .

In brief, we obtained 11 stable and one high-temperature stable  $M_3A_2X$  phases in thermodynamics from 240  $M_3A_2X$  candidates. The crystal structure information (crystal system, space group, lattice parameters, and atomic coordinates) of these 12 stable  $M_3A_2X$  phases is listed in Table S.4 [64]. Among them, nine phases are newly discovered and have never been reported before. In particular, crystal structure [trigonal,  $P\bar{3}m1$ , Fig. 1(e)] of  $Sc_3S_2C$ ,  $Y_3S_2C$ , and  $Y_3Se_2C$  are novel and different from that [hexagonal,  $P6_3/mmc$ , Fig. 1(d)] of synthesized  $M_3A_2X$  phases [31].

It is particularly noteworthy that thermodynamically unstable  $M_3A_2X$  phases with positive  $E_{comp}$  values in Table S.3 [64] can also be experimentally synthesized. Approximately 20% of the compounds in the Inorganic Crystal Structure Database [74] exhibit formation energies exceeding 0.036 eV/atom. Some top-down approaches (such as molten salt synthesis) [13] or thin film processing [15] can obtain metastable or far from thermodynamically stable  $M_3A_2X$  phases [1,3,4].

## 2. Dynamic stability

Dynamic stability of a phase refers to the ability of its crystal structure against small atomic displacements and can be judged from no imaginary frequencies in its phonon dispersion spectrum. The calculated phonon dispersion spectra of all 12 thermodynamically stable  $M_3A_2X$  phases are presented in Fig. S.3 [64].  $Nb_3As_2C$  and  $Y_3S_2C$ , as representatives of the

FIG. 8. Phonon dispersion spectra of  $\text{Nb}_3\text{As}_2\text{C}$  and  $\text{Y}_3\text{S}_2\text{C}$  phases.

No. 4 and 51 configurations, respectively, have their phonon dispersion spectra shown in Fig. 8. No imaginary frequencies were observed within the whole phonon dispersion ranges of the 12  $M_3A_2X$  phases, indicating dynamic stability.

### 3. Mechanical stability

Mechanical stability, which refers to the ability of a structure to resist deformations or distortions in terms of strain, can be evaluated by checking whether its elastic constants meet the Born stability conditions. For hexagonal system (No. 4 configuration,  $P6_3/mmc$ ), its five independent elastic constants ( $C_{11}$ ,  $C_{12}$ ,  $C_{13}$ ,  $C_{33}$ ,  $C_{44}$ ) should meet the stability criterion:  $C_{11} > 0$ ,  $C_{44} > 0$ ,  $C_{11} > C_{12}$ ,  $(C_{11} + C_{12})C_{33} - 2C_{13}^2 > 0$ . For a trigonal system (No. 51 configuration,  $P\bar{3}m1$ ), its six independent elastic constants ( $C_{11}$ ,  $C_{12}$ ,  $C_{13}$ ,  $C_{14}$ ,  $C_{33}$ ,  $C_{44}$ ) should meet the stability criterion:  $C_{11} > 0$ ,  $C_{44} > 0$ ,  $C_{11} > C_{12}$ ,  $(C_{11} + C_{12})C_{33} - 2C_{13}^2 > 0$ ,  $(C_{11} - C_{12})C_{44} - 2C_{14}^2 > 0$ . Elastic constants of the 12 thermodynamically stable  $M_3A_2X$  phases are given in Table II. The elastic constants of all the 12  $M_3A_2X$  phases satisfy the above criteria, indicating their mechanical stabilities.

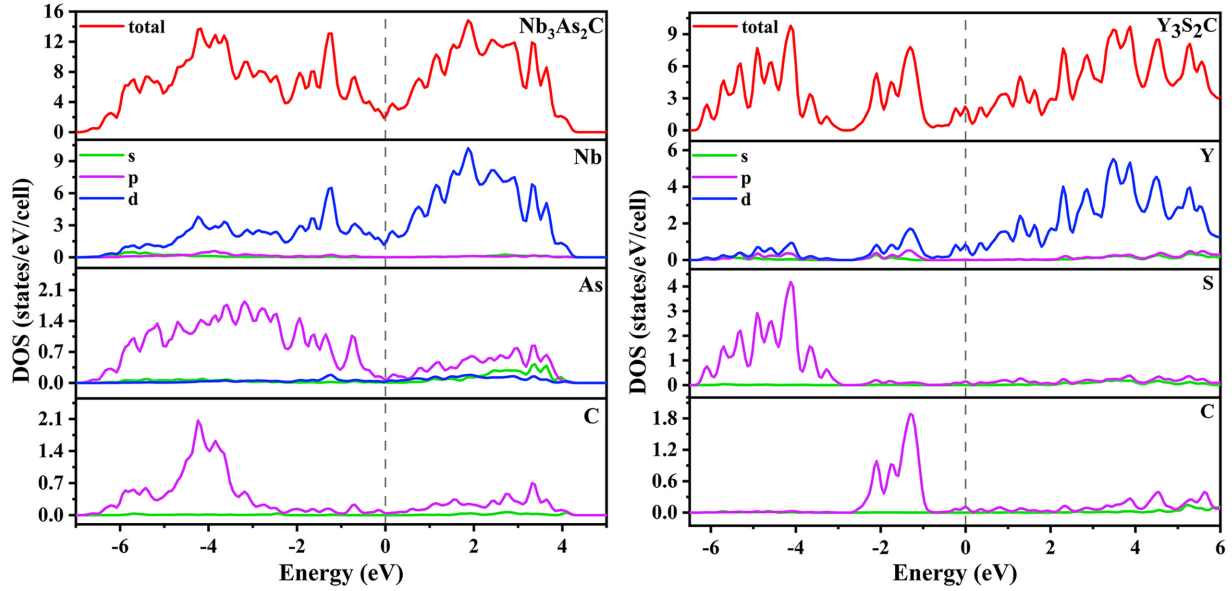
### D. Electronic properties

Band structures and density of states (DOS) of the 12 thermodynamically stable  $M_3A_2X$  phases were calculated to evaluate their electronic properties, as depicted in Fig. S.4 and Fig. S.5 [64].  $\text{Nb}_3\text{As}_2\text{C}$  and  $\text{Y}_3\text{S}_2\text{C}$ , as representatives of the No. 4 and 51 configurations, respectively, have their DOS curves shown in Fig. 9. All 12  $M_3A_2X$  phases exhibit metallic conductivity, which mainly comes from the  $d$  electron of  $M$  atoms. From the local DOS presented in Fig. 9, the bonding states of  $M$ -A and  $M$ -C can be discerned through the hybridization between the  $d$  orbitals of  $M$  atoms and the  $p$  orbitals of A atoms or the  $p$  orbitals of C atoms.

For a class of materials with similar crystal structures, the DOS at Fermi level can be used to quantitatively compare their relative electrical conductivities [71]. Figure 10 illustrates the DOS values at the Fermi level of the 12 stable  $M_3A_2X$  phases in comparison with their corresponding  $M_2AX$  phases. Previous work [71] has indicated that the DOS at Fermi level is reasonably correlated with the total valence electron number per volume. However, this correlation in  $M_3A_2X$  and  $M_2AX$  is not clearly discernible from Fig. 10. Perhaps this is due to the relatively small number of phases in the calculation of DOS. We observed that the DOS values at Fermi level for the

TABLE II. Elastic constants of the 12 thermodynamically stable  $M_3A_2X$  phases (GPa).

| Phase                            | Crystal system | $C_{11}$ | $C_{12}$ | $C_{13}$ | $C_{14}$ | $C_{33}$ | $C_{44}$ | $C_{66}$ |
|----------------------------------|----------------|----------|----------|----------|----------|----------|----------|----------|
| $\text{Sc}_3\text{S}_2\text{C}$  | Trigonal       | 219.98   | 59.26    | 63.66    | -15.93   | 191.68   | 85.77    | 80.36    |
| $\text{Y}_3\text{S}_2\text{C}$   | Trigonal       | 186.36   | 51.55    | 60.43    | -18.87   | 159.66   | 77.11    | 67.40    |
| $\text{Y}_3\text{Se}_2\text{C}$  | Trigonal       | 160.48   | 47.70    | 55.54    | -18.27   | 143.61   | 66.92    | 56.39    |
| $\text{Zr}_3\text{S}_2\text{C}$  | Hexagonal      | 264.92   | 88.11    | 98.49    | —        | 293.62   | 132.47   | 88.41    |
| $\text{Zr}_3\text{Se}_2\text{C}$ | Hexagonal      | 234.50   | 76.85    | 91.56    | —        | 256.14   | 121.44   | 78.82    |
| $\text{Hf}_3\text{S}_2\text{C}$  | Hexagonal      | 294.80   | 91.51    | 108.26   | —        | 310.00   | 145.81   | 101.65   |
| $\text{Hf}_3\text{Se}_2\text{C}$ | Hexagonal      | 260.67   | 79.40    | 98.74    | —        | 268.43   | 130.13   | 90.63    |
| $\text{V}_3\text{P}_2\text{C}$   | Hexagonal      | 339.52   | 107.44   | 158.73   | —        | 398.52   | 207.19   | 116.04   |
| $\text{Nb}_3\text{As}_2\text{C}$ | Hexagonal      | 295.90   | 101.42   | 141.37   | —        | 341.48   | 168.01   | 97.24    |
| $\text{Nb}_3\text{P}_2\text{C}$  | Hexagonal      | 332.44   | 109.95   | 153.93   | —        | 395.49   | 186.79   | 111.24   |
| $\text{Ta}_3\text{As}_2\text{C}$ | Hexagonal      | 316.97   | 108.25   | 153.46   | —        | 368.69   | 179.84   | 104.36   |
| $\text{Ta}_3\text{P}_2\text{C}$  | Hexagonal      | 355.57   | 118.79   | 169.15   | —        | 424.50   | 203.27   | 118.39   |

FIG. 9. Local density of states (LDOS) of  $\text{Nb}_3\text{As}_2\text{C}$  and  $\text{Y}_3\text{S}_2\text{C}$  phases.

majority of  $M_3A_2X$  phases (nine out of 12) are higher than those of their corresponding  $M_2AX$  phases. This implies that  $M_3A_2X$  phases have generally better electrical conductivity than  $M_2AX$  phases. Among the stable  $M_3A_2X$  phases,  $\text{V}_3\text{P}_2\text{C}$  has the best electrical conductivity.

### E. Mechanical properties

Micromechanical properties, such as bulk and shear moduli, are of great significance because they play an important role in macromechanical properties, including lubrication, friction, and machinability. Experimental investigation into the micromechanical properties of the MAX phase has been obstructed by the difficulties in obtaining pure samples. The micromechanical properties of polycrystalline samples can be calculated from the corresponding elastic constants according to so-called Voigt-Reuss-Hill approximations. The Voigt and Reuss values represent the upper and lower limits of the elastic

constants of polycrystalline, respectively. The Hill value is the average of the Voigt and Reuss values, and thus can be thought of as practical estimates.

The bulk modulus ( $B$ ) serves as a metric for the volume compressibility of a material, and the shear modulus ( $G$ ) measures the average shearability of the material, which can be obtained as follows:

$$B_V = [(C_{11} + C_{22} + C_{33}) + 2(C_{12} + C_{13} + C_{23})]/9,$$

$$G_V = [(C_{11} + C_{22} + C_{33}) - (C_{12} + C_{13} + C_{23}) + 3(C_{44} + C_{55} + C_{66})]/15,$$

$$B_R = 1/[(S_{11} + S_{22} + S_{33}) + 2(S_{12} + S_{13} + S_{23})],$$

$$G_R = 15/[4(S_{11} + S_{22} + S_{33}) - 4(S_{12} + S_{13} + S_{23}) + 3(S_{44} + S_{55} + S_{66})],$$

$$B = B_H = (B_V + B_R)/2, \quad G = G_H = (G_V + G_R)/2,$$

where  $S_{ij}$  is the elastic compliance, and the subscripts V, R, and H denote the Voigt, Reuss, and Hill moduli, respectively. The Young's modulus ( $E$ ), Poisson's ratio ( $\nu$ ), and Pugh's ratio ( $k$ ) can be calculated using the following equations:

$$E = 9BG/(3B + G), \quad \nu = (3B - 2G)/(6B + 2G), \quad k = G/B.$$

The Vickers hardness ( $H_V$ ) is taken as the average value of the hardness values (see Table S.5 [64]) calculated by the following four formulas [75–78]:

$$H_{\text{Chen}} = 2(k^2G)^{0.585} - 3, \quad H_{\text{Tian}} = 0.92k^{1.137}G^{0.708}, \quad H_{\text{Miao}} = (1-2\nu)E/[6(1+\nu)], \quad H_{\text{Jiang}} = G/6.78.$$

The data of micromechanical properties of the 12 stable  $M_3A_2X$  phases are presented in Table III. For greater intuitiveness, the  $B$  and  $G$  moduli are plotted in Figs. 11(a) and 11(b). The  $B$  ( $G$ ) value spreads in a wide range and varies from 86.9 (57.9) GPa in  $\text{Y}_3\text{Se}_2\text{C}$  to 225.3 (144.2) GPa in  $\text{Ta}_3\text{P}_2\text{C}$ , indicating broad potential applications in various areas. The  $B$  value of  $\text{Ta}_3\text{P}_2\text{C}$  is higher than those of four

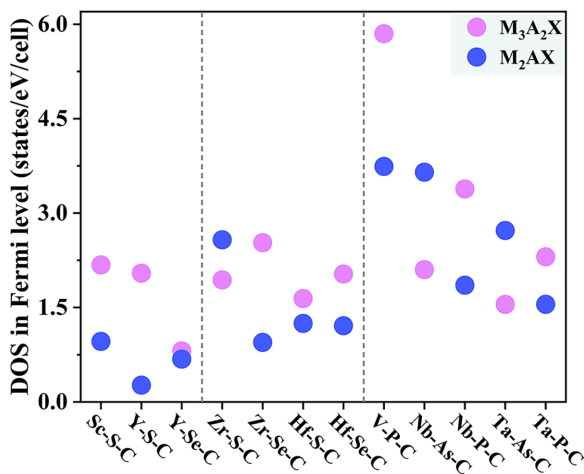
FIG. 10. DOS values at Fermi level of the 12 stable  $M_3A_2X$  phases in comparison with their corresponding  $M_2AX$  phases.

TABLE III. Calculated bulk modulus  $B$  (GPa), shear modulus  $G$  (GPa), Young's modulus  $E$  (GPa), Pugh's ratio  $k$ , Poisson's ratio  $\nu$ , Vickers hardness  $H_V$  (GPa) of the 12 stable  $M_3A_2X$  phases in comparison with their corresponding  $M_2AX$  phases.

| Phase                             | $B$   | $G$   | $E$   | $k$  | $\nu$ | $H_V$ | Phase               | $B$   | $G$   | $E$   | $k$  | $\nu$ | $H_V$ |
|-----------------------------------|-------|-------|-------|------|-------|-------|---------------------|-------|-------|-------|------|-------|-------|
| Sc <sub>3</sub> S <sub>2</sub> C  | 111.5 | 79.7  | 193.2 | 0.72 | 0.21  | 13.9  | Sc <sub>2</sub> SC  | 125.7 | 91.0  | 219.9 | 0.72 | 0.21  | 15.7  |
| Y <sub>3</sub> S <sub>2</sub> C   | 97.3  | 67.6  | 164.8 | 0.70 | 0.22  | 11.8  | Y <sub>2</sub> SC   | 104.0 | 71.9  | 175.3 | 0.69 | 0.22  | 12.3  |
| Y <sub>3</sub> Se <sub>2</sub> C  | 86.9  | 57.9  | 142.0 | 0.67 | 0.23  | 9.9   | Y <sub>2</sub> SeC  | 97.3  | 67.1  | 163.6 | 0.69 | 0.22  | 11.6  |
| Zr <sub>3</sub> S <sub>2</sub> C  | 154.5 | 104.6 | 256.0 | 0.68 | 0.22  | 16.7  | Zr <sub>2</sub> SC  | 164.2 | 113.1 | 275.8 | 0.69 | 0.22  | 18.1  |
| Zr <sub>3</sub> Se <sub>2</sub> C | 138.0 | 93.1  | 228.1 | 0.68 | 0.23  | 15.1  | Zr <sub>2</sub> SeC | 151.7 | 103.4 | 252.9 | 0.68 | 0.22  | 16.7  |
| Hf <sub>3</sub> S <sub>2</sub> C  | 168.2 | 116.0 | 283.0 | 0.69 | 0.22  | 18.5  | Hf <sub>2</sub> SC  | 177.1 | 125.7 | 304.9 | 0.71 | 0.21  | 20.4  |
| Hf <sub>3</sub> Se <sub>2</sub> C | 149.1 | 102.3 | 249.7 | 0.69 | 0.22  | 16.6  | Hf <sub>2</sub> SeC | 162.3 | 114.5 | 278.0 | 0.71 | 0.21  | 18.8  |
| V <sub>3</sub> P <sub>2</sub> C   | 211.9 | 142.5 | 349.2 | 0.67 | 0.23  | 21.6  | V <sub>2</sub> PC   | 232.1 | 149.0 | 368.2 | 0.64 | 0.24  | 21.5  |
| Nb <sub>3</sub> As <sub>2</sub> C | 187.5 | 118.0 | 292.7 | 0.63 | 0.24  | 17.4  | Nb <sub>2</sub> AsC | 204.4 | 120.5 | 302.1 | 0.59 | 0.25  | 16.9  |
| Nb <sub>3</sub> P <sub>2</sub> C  | 208.6 | 134.7 | 332.5 | 0.65 | 0.23  | 20.0  | Nb <sub>2</sub> PC  | 223.3 | 139.4 | 346.2 | 0.62 | 0.24  | 20.0  |
| Ta <sub>3</sub> As <sub>2</sub> C | 201.8 | 126.3 | 313.6 | 0.63 | 0.24  | 18.4  | Ta <sub>2</sub> AsC | 219.1 | 128.8 | 323.0 | 0.59 | 0.25  | 17.9  |
| Ta <sub>3</sub> P <sub>2</sub> C  | 225.3 | 144.2 | 356.4 | 0.64 | 0.24  | 21.0  | Ta <sub>2</sub> PC  | 240.3 | 148.4 | 369.2 | 0.62 | 0.24  | 21.1  |

synthesized  $M_3A_2X$  phases and close to the known maximum value (Ta<sub>4</sub>AlC<sub>3</sub>, 266 GPa) [34] of MAX phases. From Figs. 11(a) and 11(b), we noticed that the  $B$  and  $G$  values depend on  $M$  and  $A$  elements. As the  $M$  element ranges from Group IIIB to VB, the values of  $B$  and  $G$  gradually increase.

For the  $A$  element from Group VA to VIA, the trends of  $B$  and  $G$  values are reversed. Our findings are consistent with the previous results about traditional MAX phases [70,79], in which elastic properties were found to be dependent on valence electrons of the constituent elements.

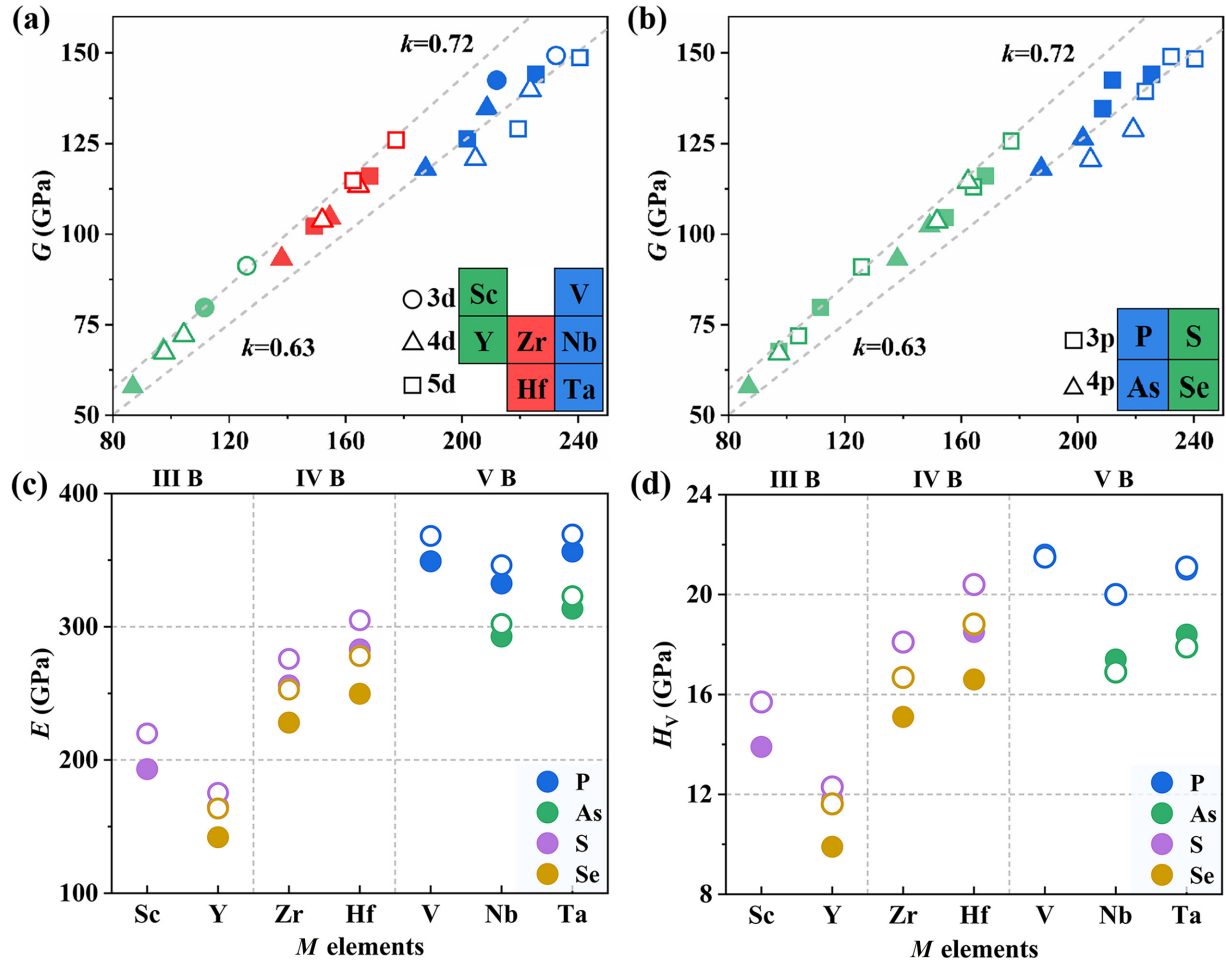


FIG. 11. (a), (b) Bulk modulus ( $B$ ), shear modulus ( $G$ ), (c) Young's modulus ( $E$ ) and (d) Vickers hardness ( $H_V$ ) of the 12 stable  $M_3A_2X$  phases in comparison with their corresponding  $M_2AX$  phases. The solid and empty symbols represent the  $M_3A_2X$  and  $M_2AX$  phases, respectively.

The Young's modulus ( $E$ ) serves as a crucial indicator of a material's stiffness. Since  $E$  is calculated from  $B$  and  $G$ , it exhibits the same variation trend as  $B$  and  $G$  [seen from Fig. 11(c)]. The Vickers hardness [ $H_V$  shown in Fig. 11(d)] ranges from 9.9 to 21.6 GPa. The  $M_3A_2X$  phases with  $M$  in Group VB exhibit high hardness, in which,  $V_3P_2C$  has the highest hardness of 21.6 GPa. Poisson's ratio ( $\nu$ ) provides the overall bonding characteristics of a material. Since the  $M$  and  $A$  elements in the 12 stable  $M_3A_2X$  phases are narrowly distributed in the periodic table, the bond characteristics of these phases are similar. As a result, their Poisson's ratio values are close and fall within a narrow range from 0.21 to 0.24. Pugh's ratio ( $k$ ) can identify the brittleness and ductility of a material. A higher Pugh's ratio ( $>0.57$ ) indicates that the material is more likely to be brittle, while a lower ratio ( $<0.57$ ) suggests greater ductility. The  $k$  of the 12  $M_3A_2X$  phases falls within the narrow range of 0.63–0.72 [seen from Figs. 11(a) and 11(b)], indicating that all of them are brittle.

We calculated the micromechanical properties of traditional  $M_2AX$  phases and compared their results with those of the  $M_3A_2X$  phases, as shown in Table III and Fig. 11. In Figs. 11(a) and 11(b), the  $B$  and  $G$  values of  $M_3A_2X$  are located in the lower-left corner of the corresponding  $M_2AX$ , indicating that the  $B$  and  $G$  of  $M_3A_2X$  are weaker than those of  $M_2AX$ . Correspondingly, all  $E$  values and most  $H_V$  values of  $M_3A_2X$  are lower than those of  $M_2AX$ . Only the  $H_V$  values of  $M_3A_2X$  with  $M$  in Group VB are slightly higher. Overall, the mechanical properties of the  $M_3A_2X$  phases are slightly weaker than those of the  $M_2AX$  phases.

Theoretical mechanical properties of a material depend on its crystal structure and the constituent chemical bonds. Considering that  $M_3A_2X$  and  $M_2AX$  have similar crystal structures, bond strength plays a crucial role in determining the mechanical properties. The COHP analysis was carried out to compare the bond strength in  $M_3A_2X$  and  $M_2AX$ . The bonding strength can be determined quantitatively by integrating the bonding states of the -COHP curves up to the Fermi level. A larger -ICOHP value implies a stronger bond.

Figure 12(a) illustrates the -ICOHP values of the  $M$ - $C$  and  $M$ - $A$  bonds of the 12 stable  $M_3A_2X$  phases in comparison with their corresponding  $M_2AX$  phases. It should be noted that there are two types of  $M$ - $A$  bonds in  $M_3A_2X$ :  $M1$ - $A$  and  $M2$ - $A$  (see Fig. 1). The -ICOHP values of  $M$ - $A$  and  $M$ - $C$  bonds in  $M_3A_2X$  are higher when  $M$  is in Group VB than in Group IIIB or IVB, suggesting stronger bonds in the former case. This finding is highly consistent with the previous results of mechanical properties. Compared with the  $M$ - $A$  bonds in  $M_2AX$ , the  $M1$ - $A$  bonds in the corresponding  $M_3A_2X$  become stronger, while the  $M2$ - $A$  bonds are weaker. Meanwhile, the  $M$ - $C$  bonds in  $M_3A_2X$  are weaker than those in the corresponding  $M_2AX$  phase. Overall, the atomic interactions in  $M_3A_2X$  are slightly weaker than those in the corresponding  $M_2AX$ . As a result,  $M_3A_2X$  has slightly inferior mechanical properties to  $M_2AX$ .

The  $M$ - $C$  and  $M$ - $A$  bond lengths in both  $M_3A_2X$  and  $M_2AX$  are presented in Fig. 12(b). Upon careful observation, it can be found that, compared with the  $M_2AX$  phase, the variation trend of the bond length in  $M_3A_2X$  is opposite to that of the bond strength. As shown in Fig. 12(c), there is basi-

cally an inverse relationship between the bond length and the bond strength of the  $MAX$  phases. This indicates that for the same type of chemical bonds, bond length, to some extent, can reflect bond strength, which is also in line with general knowledge.

## F. Magnetic properties

To check magnetic properties of the 12 stable  $M_3A_2X$  phases, we calculated their spin-resolved DOS (see Fig. S.6 [64]). The spin-up and spin-down states for each stable  $M_3A_2X$  phase are completely symmetric and the magnetic moments of all the 12  $M_3A_2X$  are  $0\mu_B$ , indicating their nonmagnetic properties.  $Mn_2GaC$  is the first experimentally discovered  $MAX$  phase with magnetism [80]. We also calculated the spin-resolved DOS of  $Mn_2GaC$  (see Fig. S.7 [64]). Its spin-up and spin-down states are asymmetric, displaying ferromagnetic state. The total and Mn magnetic moments are calculated to be 6.69 and  $1.78\mu_B$ , which is consistent with experiment result [80]. The discovered magnetic  $MAX$  phases contained either Mn or Cr [81]. However, among the 12 stable  $M_3A_2X$  phases we predicted, none include the above two elements. Therefore, it is reasonable that they do not exhibit magnetism.

## G. Exfoliation of the $M_3A_2X$ phases to form 2D MXenes

As previously mentioned,  $MAX$  phases can be exfoliated into 2D MXenes. In addition to static exfoliation energy [40,82–84], bond strengths represented by force constant [40,82,84] or COHP [82,84] have been used to explore the exfoliation potential of  $MAX$  phases to form 2D MXenes. In this section, we used the above calculated COHP results to investigate the exfoliation possibility of the 12 stable  $M_3A_2X$  phases by physical exfoliation methods.

As can be seen in Fig. 12(a), the  $M$ - $C$  bonds are significantly stronger than the  $M$ - $A$  bonds, which is the reason 2D MXenes were prepared by cleaving the  $M$ - $A$  bonds in  $MAX$  phases. Weak  $M$ - $A$  bonds are the primary condition for exfoliating  $MAX$  phases. However, this condition alone is inadequate. It is also required that the  $M$ - $C$  bonds should be relatively strong. Otherwise, the  $MAX$  phases will completely collapse to form other bulk materials during exfoliation and will not be able to retain the 2D MXene sheets. Thus we use the -ICOHP ratio of  $M$ - $A$  bond to  $M$ - $C$  bond to represent the ease of exfoliation of  $MAX$  phases in forming 2D MXenes. Lower -ICOHP ratio values indicate a higher possibility of exfoliation.

Figure 12(d) illustrates the -ICOHP ratios of  $M$ - $A$  bonds to  $M$ - $C$  bonds of the 12 stable  $M_3A_2X$  phases and their corresponding  $M_2AX$  phases. The -ICOHP ratios of all  $M_3A_2X$  and  $M_2AX$  are  $< 1$ , meaning that  $M$ - $A$  bonds are weaker than  $M$ - $C$  bonds. Since  $M$ - $A$  bonds in  $M_2AX$  are weaker than  $M1$ - $A$  bonds but stronger than  $M2$ - $A$  bonds in  $M_3A_2X$ , the -ICOHP ratios of  $M$ - $A$  to  $M$ - $C$  in  $M_2AX$  are smaller than those of  $M1$ - $A$  to  $M$ - $C$  in  $M_3A_2X$ , yet larger than those of  $M2$ - $A$  to  $M$ - $C$  bonds in  $M_3A_2X$ . During the exfoliation process, the  $M2$ - $A$  bonds in  $M_3A_2X$  are preferentially cleaved. Therefore,  $M_3A_2X$  can be more easily exfoliated into 2D MXenes than corresponding  $M_2AX$ . The  $Zr_3Se_2C$ ,  $Zr_3S_2C$ , and  $Sc_3S_2C$  phases exhibit the

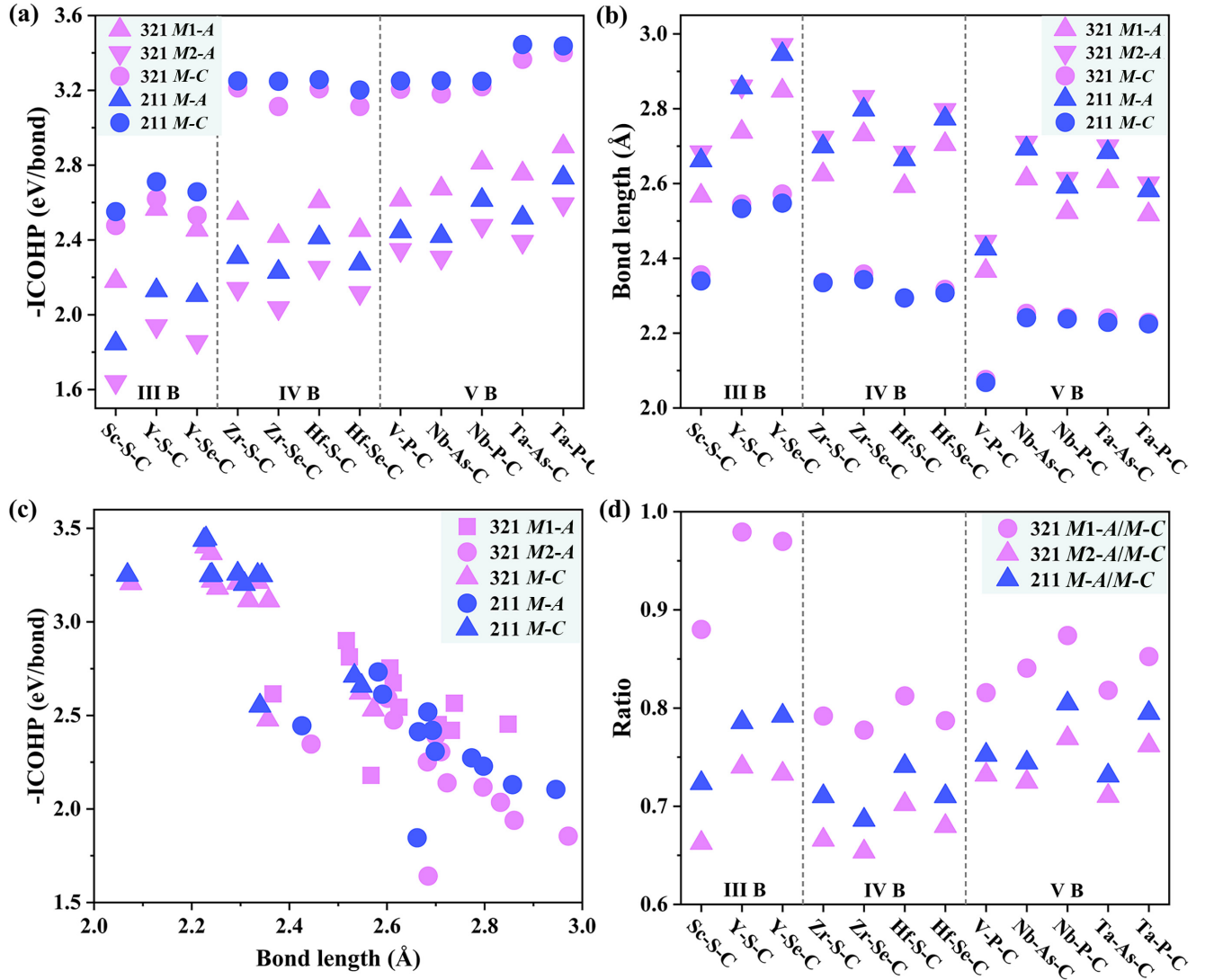


FIG. 12. (a) Bond -ICOHP values, (b) bond lengths, (c) bond -ICOHP values as a function of bond lengths, and (d) bond -ICOHP ratio of  $M-A$  to  $M-C$  of the 12 stable  $M_3A_2X$  phases and their corresponding  $M_2AX$  phases. The 321 and 211 represent  $M_3A_2X$  phase and  $M_2AX$  phase, respectively.

lowest -ICOHP ratios of  $M_2A$  to  $M-C$ . Thus, they are expected to be the most readily exfoliated. Notably, since 2D Zr- and Sc-based MXenes have not been successfully synthesized so far, the predicted stability and high exfoliation potential of the  $Zr_3Se_2C$ ,  $Zr_3S_2C$ , and  $Sc_3S_2C$  phases hold even greater practical significance.

#### IV. CONCLUSIONS

In this research, a high-throughput computational method was utilized to conduct a comprehensive investigation of the  $M_3A_2X$  phases. Through three rounds of stability assessment, 12 stable  $M_3A_2X$  phases were screened out from 240 possible compositions. Notably, nine phases are newly discovered and have never been reported before. Three ( $Sc_3S_2C$ ,  $Y_3S_2C$ , and  $Y_3Se_2C$ ) of the stable  $M_3A_2X$  phases possess novel structures distinct from those of synthesized  $M_3A_2X$  phases, which validates the necessity of considering various structures during identifying the lowest-energy structure. Our

recommendation to experimental researchers is that  $Y_3S_2C$  and  $Ta_3As_2C$  are more readily synthesizable among them. Since some  $M_3A_2X$  phases are stable only at high temperatures while some become unstable at high temperatures, the selection of temperature is crucial in experimental synthesis. Because binary  $M-A$  and  $M-X$  phases are the main competitors to the stability of  $M_3A_2X$ , it is necessary to avoid using those as raw materials during the synthesis of  $M_3A_2X$ .

Because the proportion of  $M$  atoms in  $M_3A_2X$  is higher than that in  $M_2AX$ ,  $M_3A_2X$  phases generally exhibit better electrical conductivity than their corresponding classic  $M_2AX$  phases. Among the stable  $M_3A_2X$  phases,  $V_3P_2C$  possesses the best electrical conductivity. Due to having weaker atomic interactions in  $M_3A_2X$  than  $M_2AX$ ,  $M_3A_2X$  phases demonstrate slightly inferior mechanical properties to their corresponding  $M_2AX$  phases.  $M_3A_2X$  phases possess different electrical and mechanical properties from those of known  $MAX$  phases, enabling it to identify suitable application areas.

We also investigate the exfoliation possibility of the 12 stable  $M_3A_2X$  phases through analyzing bond strength based on COHP value. The results show that  $M_3A_2X$  can be more easily exfoliated into 2D MXenes than corresponding  $M_2AX$ .  $Zr_3Se_2C$ ,  $Zr_3S_2C$ , and  $Sc_3S_2C$  are expected to be the most readily exfoliated, which holds even greater practical significance for the development of new Zr- and Sc-based MXenes.

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## DATA AVAILABILITY

The data supporting this study's findings are available within the article.

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