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¹ Bergström, Hill, and de Pasquali, *Phys. Rev.* **92**, 918 (1953).

² G. Scharff-Goldhaber, *Phys. Rev.* **90**, 487 (1953); P. Preiswerk and P. Stähelin, *Helv. Phys. Acta* **24**, 623 (1952).

³ *Handbook of Chemistry and Physics* (1952/53) (Chemical Rubber Publishing Company, Cleveland, 1952), p. 1990.

⁴ We thank Professor R. G. Wilkinson of Indiana University for his advice concerning the plating process.

⁵ F. R. Metzger and W. B. Todd, *Phys. Rev.* **95**, 853 (1954).

Self-Energy Effects on Meson-Nucleon Scattering According to the Tamm-Dancoff Method

J. C. TAYLOR

Peterhouse, Cambridge, England

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IN a paper with the foregoing title, Visscher¹ has shown that the self-energy effects in the Tamm-Dancoff method (as modified by Dyson) give rise to an unphysical pole in the meson-nucleon wave function. We show here that a simple and natural modification of the usual way of eliminating the negative frequency components removes this difficulty.

We use Visscher's notation. Define

$$\begin{aligned} X(\mathbf{p}) &= [X^+(\mathbf{p})u + X^-(\mathbf{p})w](M/E_p)^{\frac{1}{2}} \\ &= [(\Psi_0^*(0)b_{pu}a_{-p\alpha}\Psi(0))u \\ &\quad + (\Psi_0^*(0)b_{pw}a_{-p\alpha}\Psi(0))w](M/E_p)^{\frac{1}{2}}, \end{aligned}$$

where w is a negative-energy solution of the Dirac equation; and

$$-i\gamma_4(\mathbf{p} \cdot \boldsymbol{\gamma} - iM)N(p) = \frac{3}{4}iG^2\Omega_R(\mathbf{p} \cdot \boldsymbol{\gamma}),$$

where Ω_R is the finite self-energy function defined by Visscher. We suppose the meson negative-frequency components eliminated, since they are not our concern; and we leave out the meson self-energy term for simplicity. Then the second-order equation has the form

$$\begin{aligned} (\epsilon - H_p - \omega_p)[1 - \gamma_4 N(p)]X(\mathbf{p}) \\ = \int \gamma_4 K(\mathbf{p}, \mathbf{k})X(\mathbf{k})d\mathbf{k}, \quad (1) \end{aligned}$$

where $p = (\mathbf{p}, \epsilon - \omega_p)$ and K represents the interaction terms. Visscher drops negative energy components from (1), to give the approximate equation

$$\begin{aligned} (\epsilon - E_p - \omega_p)[1 - (\bar{u}(\mathbf{p})N(p)u(\mathbf{p}))M/E_p]X^+(\mathbf{p}) \\ = \int (M/E_p)^{\frac{1}{2}}(\bar{u}(\mathbf{p})K(\mathbf{p}, \mathbf{k})v(\mathbf{k}))(M/E_k)^{\frac{1}{2}}X^+(\mathbf{k})d\mathbf{k}, \quad (2) \end{aligned}$$

and a zero of the factor in the square bracket causes the unwanted pole in $X^+(\mathbf{p})$.

We propose the following alternative prescription. First transfer the square bracket in (1) to the right-hand side, then separate and drop the negative frequency components, to give

$$\begin{aligned} (\epsilon - E_p - \omega_p)X^+(\mathbf{p}) &= \int (M/E_p)^{\frac{1}{2}}(\bar{u}(\mathbf{p})\{[1 - \gamma_4 N(p)]^{-1} \\ &\quad \times K(\mathbf{p}, \mathbf{k})\}v(\mathbf{k}))(M/E_k)^{\frac{1}{2}}X^+(\mathbf{k})d\mathbf{k}. \quad (3) \end{aligned}$$

A natural further approximation gives

$$\begin{aligned} (\epsilon - E_p - \omega_p)X^+(\mathbf{p}) &= (\bar{u}(\mathbf{p})[\gamma_4 - N(p)]^{-1}u(\mathbf{p}))M/E_p \\ &\quad \times \int (M/E_p)^{\frac{1}{2}}(\bar{u}(\mathbf{p})K(\mathbf{p}, \mathbf{k})v(\mathbf{k}))(M/E_k)^{\frac{1}{2}}X^+(\mathbf{k})d\mathbf{k} \quad (4) \end{aligned}$$

as our alternative to Eq. (2).

The factor in front of the integral in (4) can be written

$$[L(u^2)]^{-1}[1 - (\bar{u}(\mathbf{p})N(-p)u(\mathbf{p}))M/E_p], \quad (5)$$

where $u = \gamma \cdot p / (iM)$, and $L(u^2)$ is a function defined by Feldman.² This is verified by noting that N is connected with Feldman's function $f(u)$ by the equation

$$-\frac{1}{3}\gamma_4 N(p) = cf(u).$$

Feldman has found the zeros of $L(u^2)$ (when $\mu = 0$), and none of them is real. Therefore, Eq. (4) does not have the difficulty of Eq. (2).

¹ W. M. Visscher, *Phys. Rev.* **96**, 788 (1954).

² G. Feldman, *Proc. Roy. Soc. (London)* **223A**, 112 (1954).

Photoproduction of π^+ Mesons from Hydrogen Near Threshold*

J. E. LEISS,† C. S. ROBINSON, AND S. PENNER

Department of Physics, University of Illinois, Urbana, Illinois

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THE total cross section for photoproduction of π^+ mesons very close to threshold has been investigated, following the method of a preliminary experiment.¹ π^+ mesons and their μ^+ decay mesons were stopped in a carbon absorber surrounding the target. Since the positrons from the decay of the stopped μ^+ mesons are emitted with an energy spectrum peaked around 36 Mev,² a large fraction will escape with considerable energy and can be counted. Since the decay of the stopped μ^+ mesons is isotropic, the positrons leaving the absorber will be essentially isotropic, regardless of the angular distribution of the emitted π^+ mesons. Except for small corrections due to geometry